

Sharing

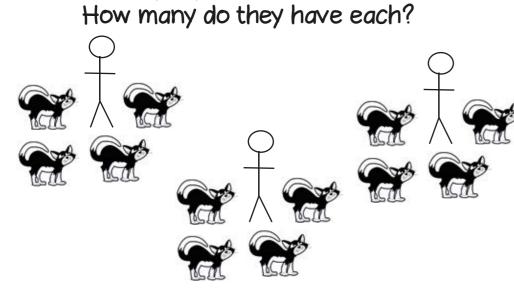
12 shared into 3 equal groups

12 ÷ 3 = 4

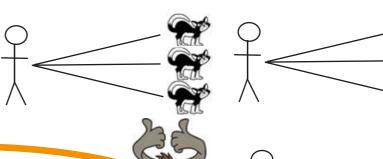
Grouping How many groups of 3 are there in 12?

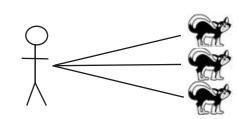
There are 12 cats.
Three people each have the same number of cats.

There are 12 cats. Each person owns 3 cats. How many people are there?



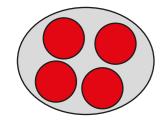
1 for you, 1 for you, 1 for you...

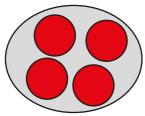


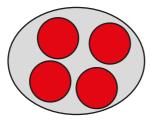


How shall I divide?

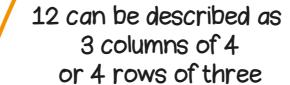


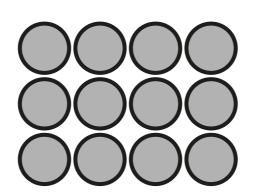


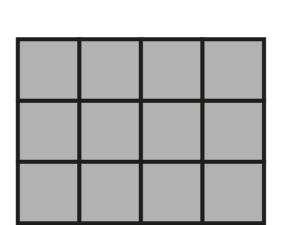


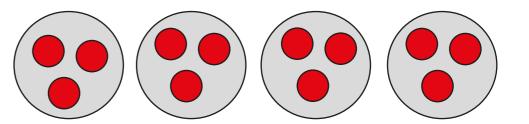


Bar model

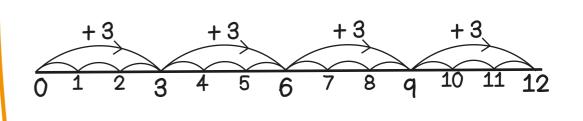




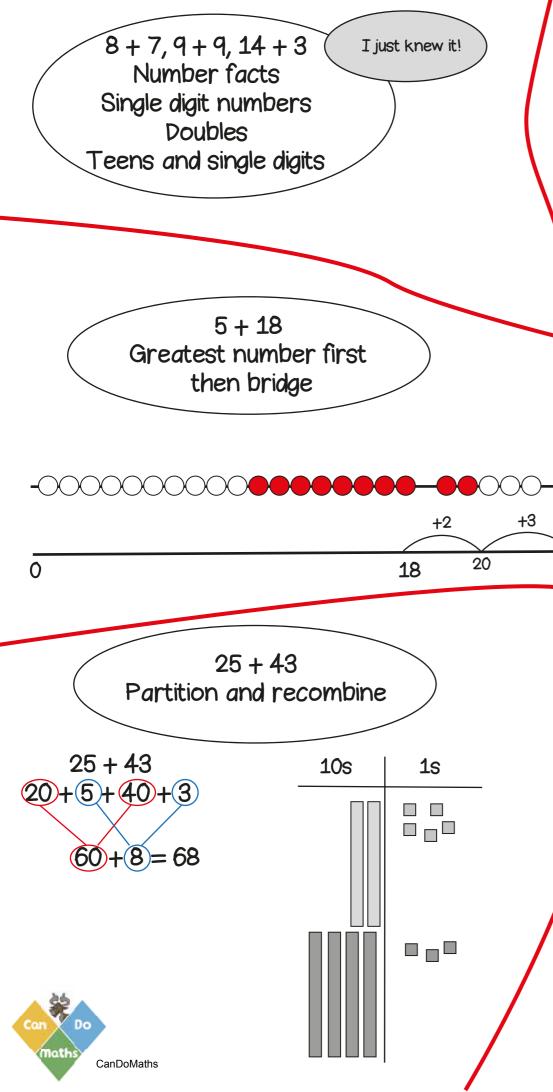


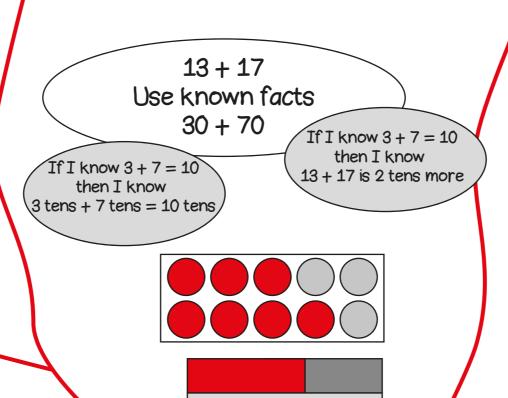


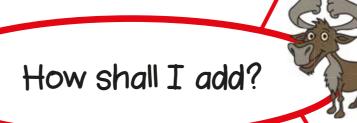


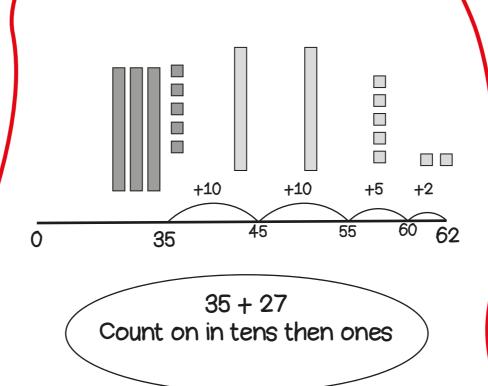




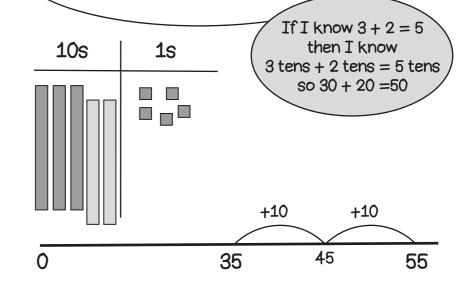


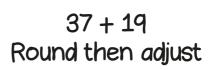


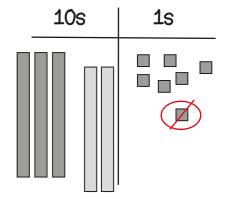




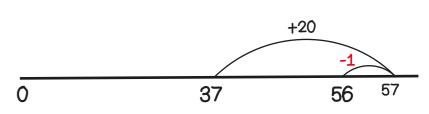
35 + 20 Add multiples of ten







Add 20 then subtract 1



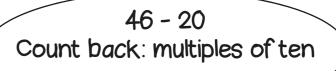


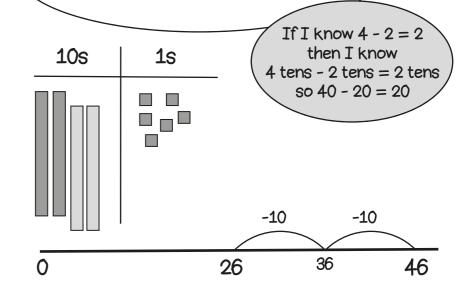
9-4, 13-5, 18-9 Number facts Single digit numbers Halves Teens and single digits

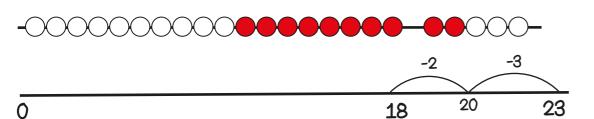
I just knew it!

23 - 5Count back: bridge through a multiple of ten

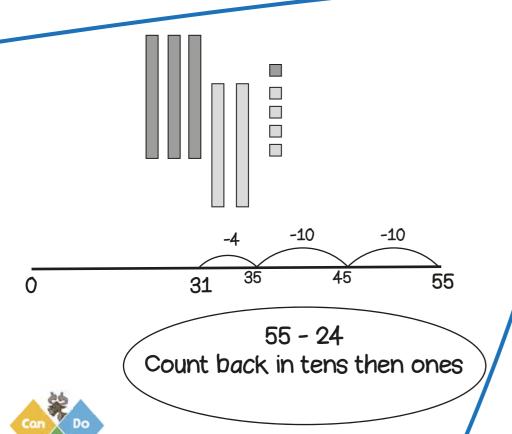
30 - 7 Use known facts 100 - 70 If I know 10 - 7 = 3then I know 30 - 7 is 2 tens and 3



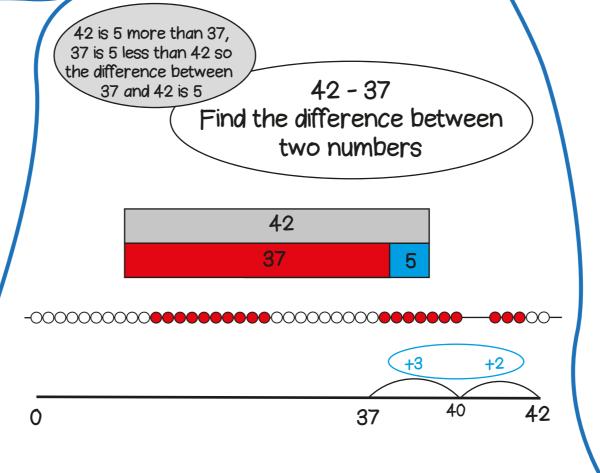


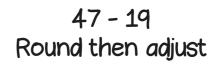


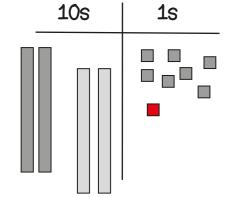
How shall I subtract?



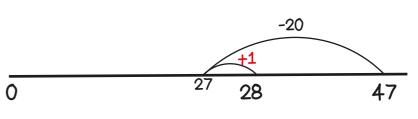
CanDoMaths





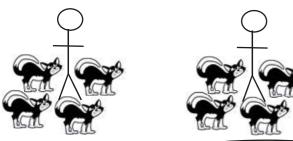


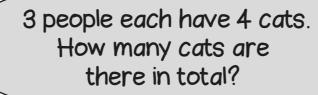
Take away 20 then add 1



Equal groups

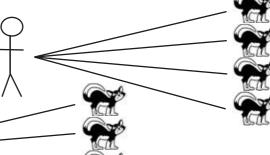
There are 3 groups with 4 cats in each group

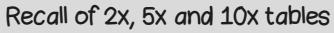




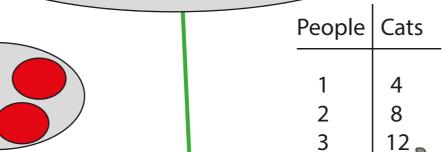
One to many correspondence

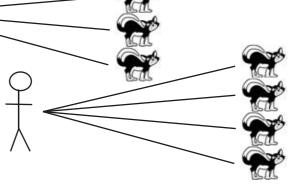
If each person has 4 cats, there are 4 times as many cats as people





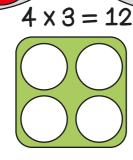






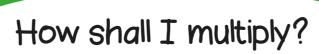


CanDoMaths

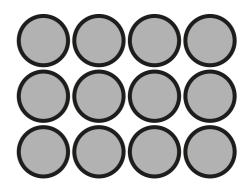


Four cats, multiplied by 3







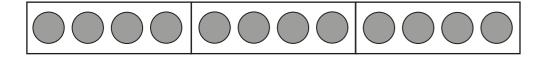


$$4 \times 3 = 12$$

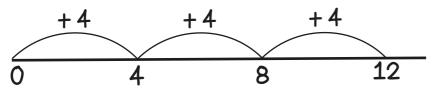
$$3 \times 4 = 4 \times 3$$



Repeated addition



4	4	4



4 + 4 + 4 = 12

Count in ones

1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12

Count in twos

2, 4, 6, 8, 10,12

Use a known fact

If 2 x 3 is 6, then 4 x 3 is double 6. Sharing

12 shared into 3 equal groups

 $12 \div 3 = 4$

Grouping

How many groups of 3 are there in 12?

There are 12 cats.

Three people each have the same number of cats.

How many do they have each?

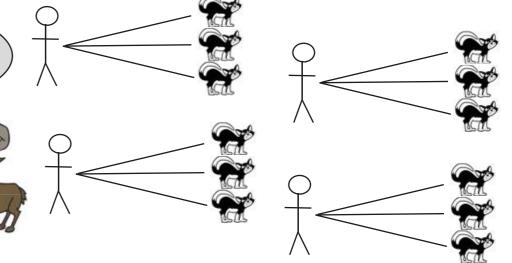
Recall and use 2x, 5x and 10x tables

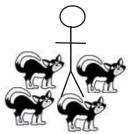
There are 12 cats. Each person owns 3 cats. How many people are there?

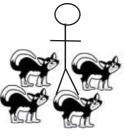


1 for you, 1 for you, 1 for you...

Grab a group of 3 grab a group of 3.

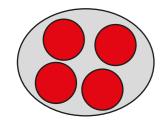


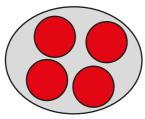


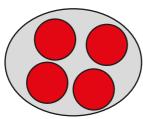




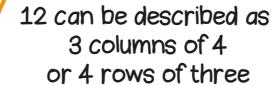
How shall I divide?

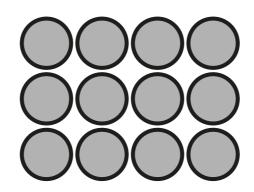


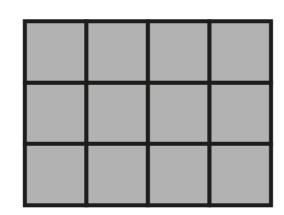


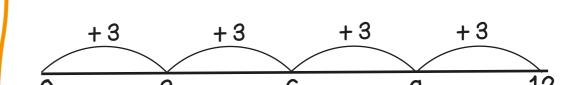


Bar model



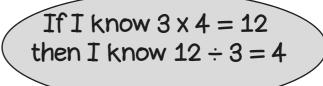


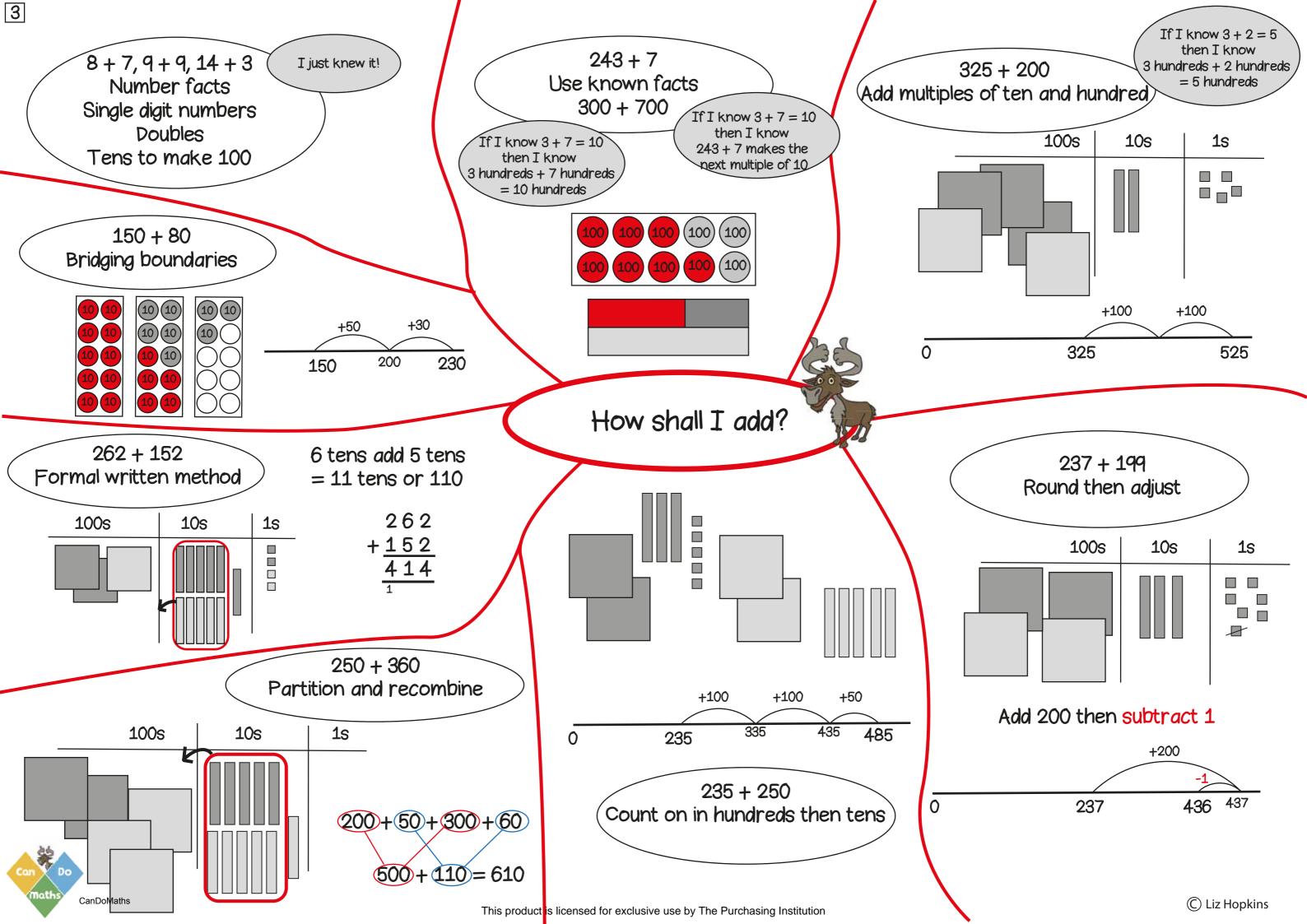


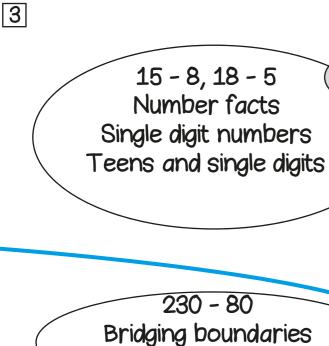


12 4

> Link to fractions. One third of 12 is 4







by counting back in efficient steps

10 10

10 10

0

10 10

I just knew it!

230 - 30 - 50 = 150

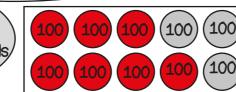
150

200

230

240 - 7 Use known facts 1000 - 700

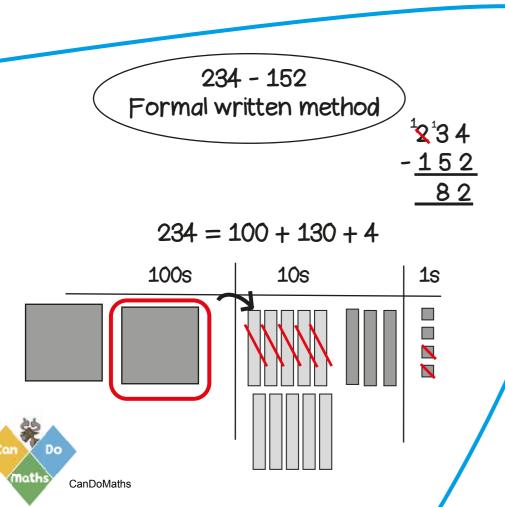
If I know 10 - 7 = 3 then I know 10 hundreds - 7 hundreds = 3 hundreds

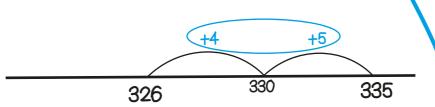


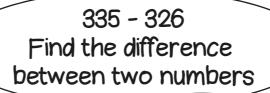
0 - 7 = 4

If I know 10 - 7 = 3
then I know
any multiple of 10,
take away 7 leaves
3 in the ones.

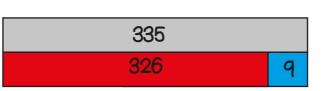
How shall I subtract?







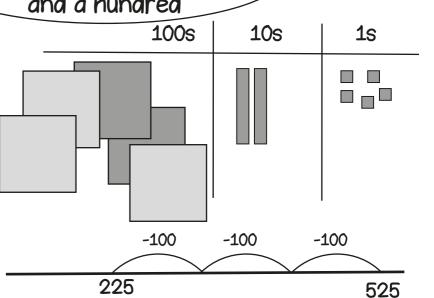
335 is 9 more than 326 326 is 9 less than 335 so the difference between them is 9



525 - 300

Take away multiples of ten

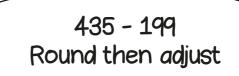
and a hundred

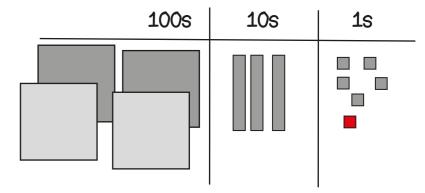


If I know 5 - 3 = 2then I know

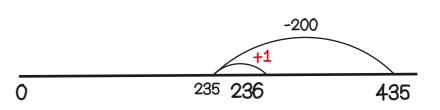
5 hundreds - 3 hundreds

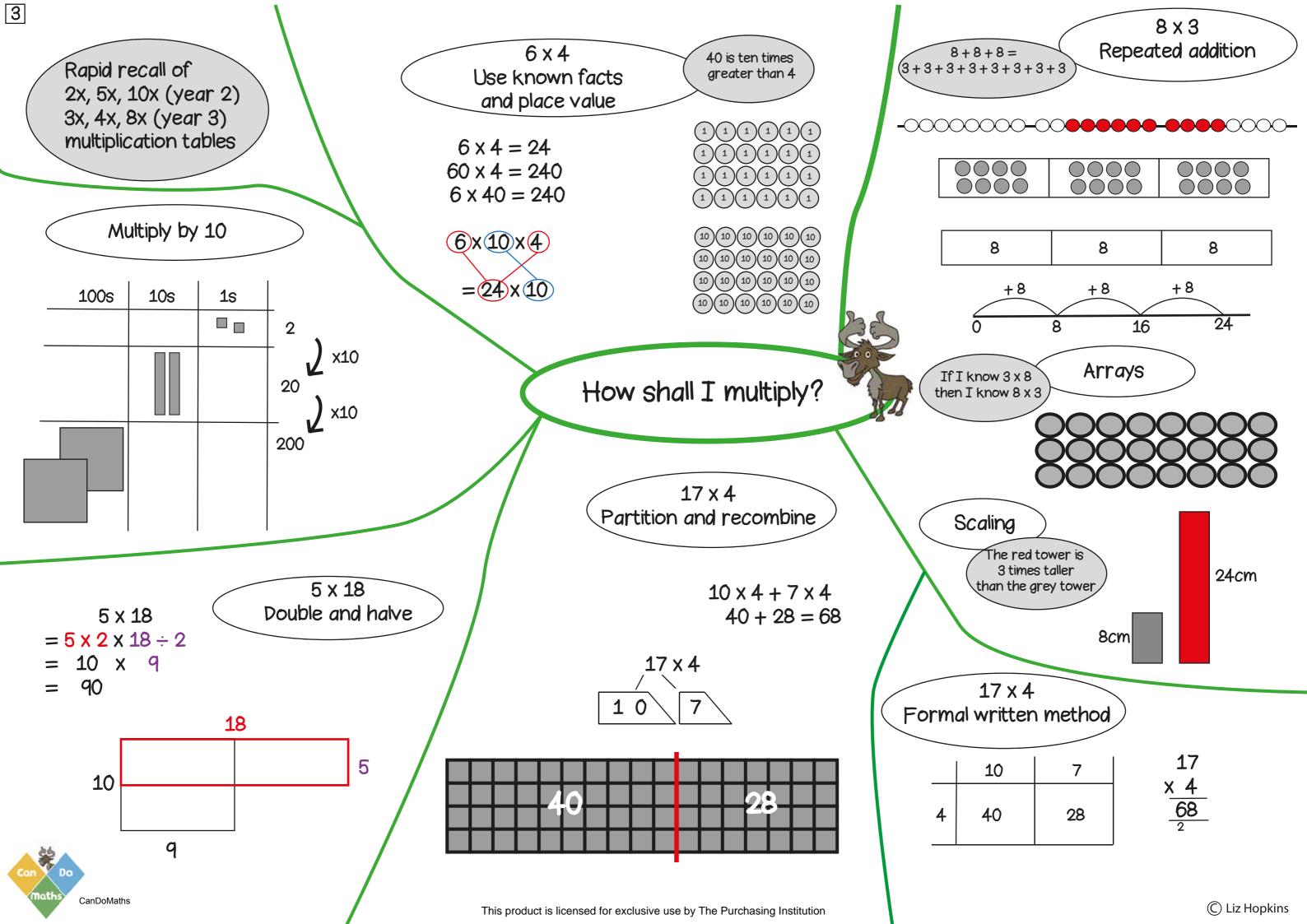
= 2 hundreds

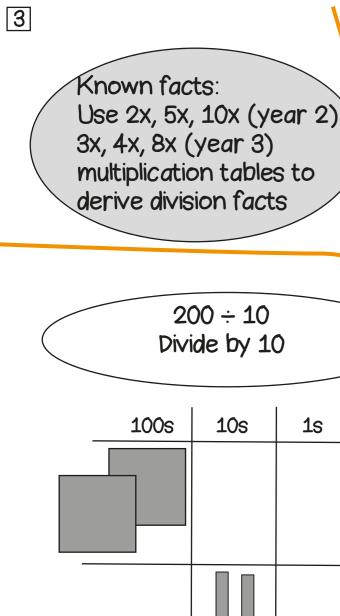




Take away 200 then add 1

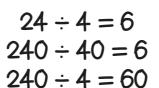






24 ÷ 4 Use known facts and place value

240 is ten times greater than 24

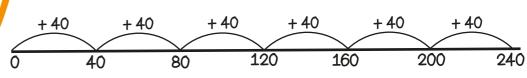


24 biscuits shared between 4 people means they will get 6 biscuits each.

If there are 10 times as many people and 10 times as many biscuits, how many biscuits each now?

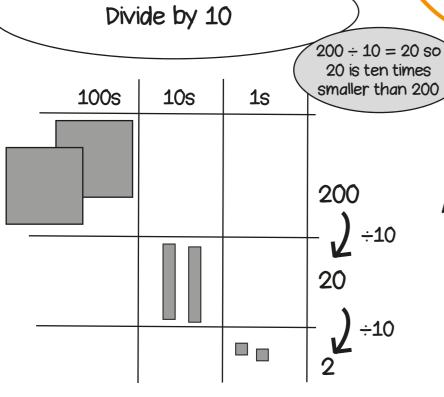


 $240 \div 40 = 6$ How many steps of 40 make 240?



45 ÷ 3

Sharing equally



How shall I divide?

A tenth of ☐ is ☐

A tenth of 1 is 1 tenth so $1 \div 10 = \frac{1}{10}$

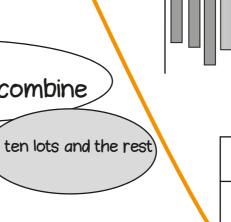
52 ÷ 4

52 ÷ 4

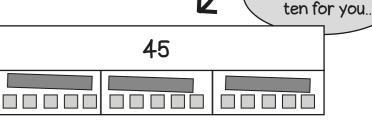
40

÷4

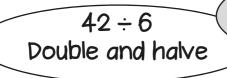
Partition and recombine



10s



10s

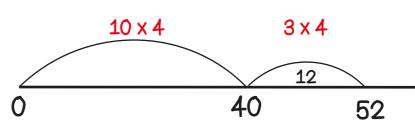


If there are half as many biscuits and half as many people...

$$42 \div 6 = 21 \div 3$$

			42		
7	7	7	7	7	7
	21				
7	7	7			

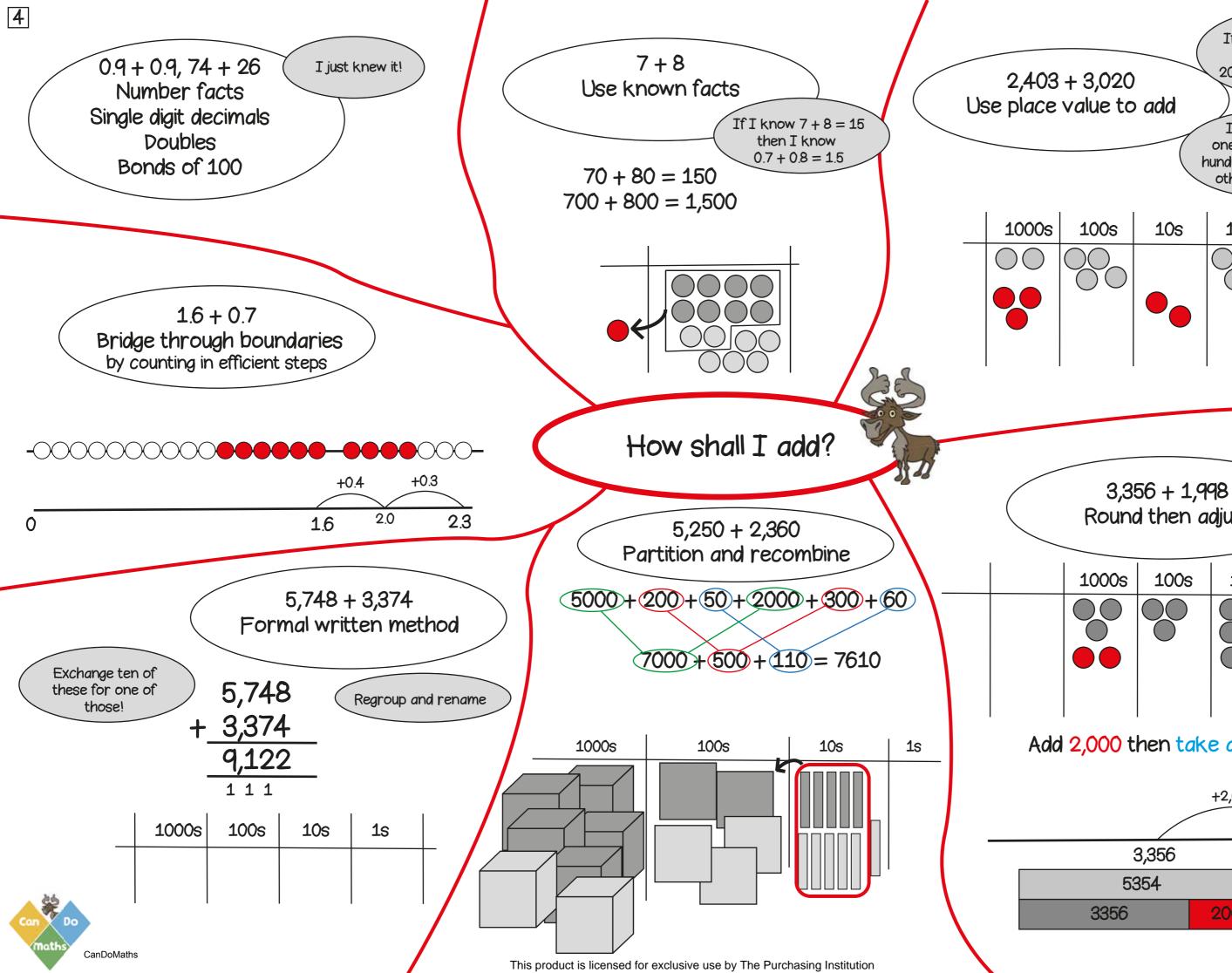
10 13



Ten for you,

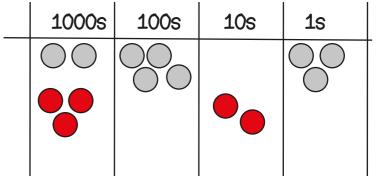
ten for you,

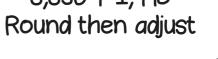
Link to fractions



If I know 2+3=5then I know 2000 + 3000 = 5000

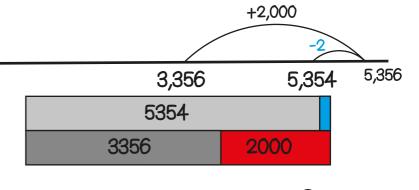
I have noticed, one number has no hundreds or ones, the other has no tens





1000s	100s	10 s	1s

Add 2,000 then take away 2



© Liz Hopkins

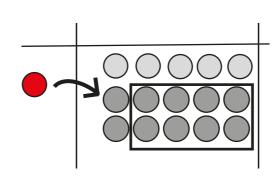
13 - 5, 1.8 - 0.8 Number facts Single digit numbers Halves Wholes and tenths

15 - 8 = 7Use known facts

> If I know 15 - 8 = 7then I know 1.5 - 0.8 = 0.7

$$150 - 80 = 70$$

 $1500 - 800 = 700$



6,342 - 3,020 Use place value to subtract

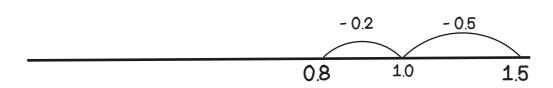
1000s

By using place value counters it is easy to see how to take away

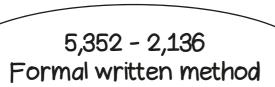
1s

10s

1.5 - 0.7Bridge through boundaries by counting in efficient steps



How shall I subtract?



I just knew it!

Exchange ten of these for one of those!

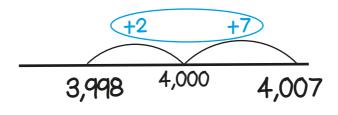
5,352 2,436

Regroup and rename

2,916

1000s	100s	10 s	1s	

4007-3998 Find the difference between two numbers



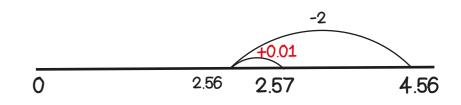
4,007	
3,998	9

4.56 - 1.99 Round then adjust

100s

1 s	$\frac{1}{10}$ S	100 s

Take away 2 then add one hundredth





Known facts: Rapid recall of all multiplication tables up to 12 x 12

6 x 4

Use known facts and place value

$$6 \times 4 = 24$$

$$0 \times 4 = 24$$

$$0 \times 4 = 24$$

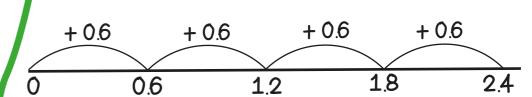
$$60 \times 4 = 240$$

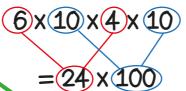
 $60 \times 40 = 2400$



40 is ten times

greater than 4





 $0.6 \times 4 = 24 \text{ tenths}$ $0.6 \times 4 = 2.4$

 $0.6 \times 4 = 2.4$

4 jumps of 0.6

0.6 is ten times

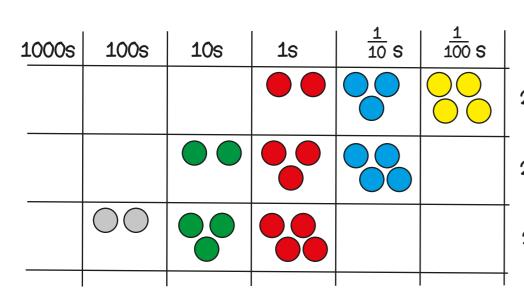
smaller than 6

36

30

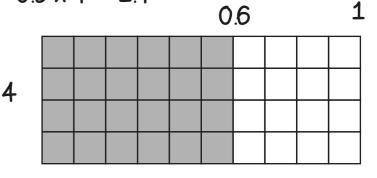
210

7



2.34 x10 23.4 x100 x10 234

How shall I multiply?

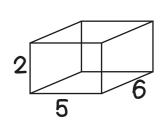


6 x 4

Use known facts

and place value

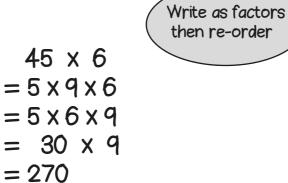
7 x 36 Use the distributive law



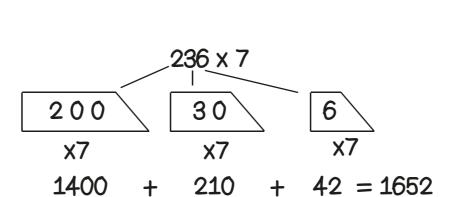
 $2 \times (5 \times 6) = (2 \times 5) \times 6$ $2 \times 30 = 10 \times 6$

45 x 6 $=5\times9\times6$ $=5\times6\times9$ $= 30 \times 9$

45 x 6 Use factors and commutativity



7 x 36) $= 7 \times 30 + 7 \times 6$ = 210 + 42= 252



36 x 7 Formal written method

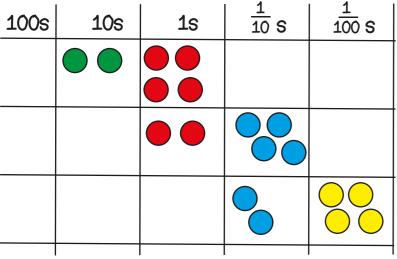
	30	6	
7	210	42	





Known facts: Use recall of all multiplication tables up to 12 x 12 to derive division facts

> 24 ÷ 100 Divide by 10, 100



24 ÷ 4 Use known facts and place value

$$24 \div 4 = 6$$

 $240 \div 40 = 6$
 $2400 \div 400 = 6$

$$2400 \div 400 = \frac{24 \times 100}{4 \times 100}$$
$$\frac{24}{4} = 6$$

240 is ten times greater than 24

24 biscuits shared between 4 people means they will get 6 biscuits each.

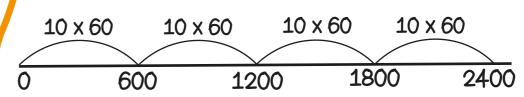
If there are 100 times as many people and 100 times as many biscuits, how many biscuits each now?

60 is ten times areater than 6

2400 ÷ 60 Use known facts and place value

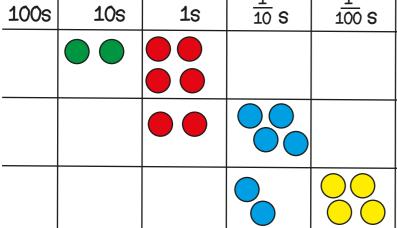
 $2400 \div 60 = 40$

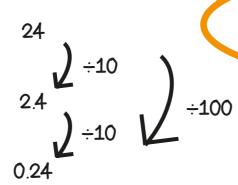
How many steps of 60 make 2400?



732 ÷ 6

Formal written method

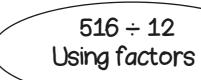




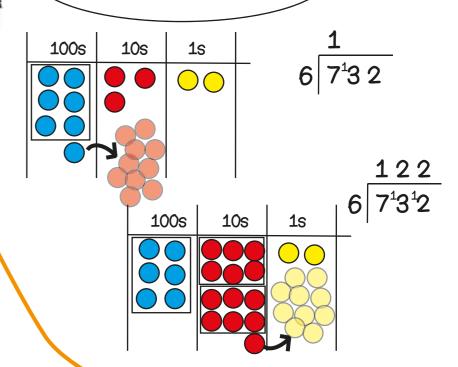
2 x 8

496

How shall I divide?

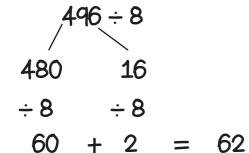


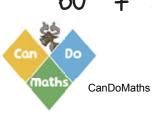
516										
	172 172				17	'2				
43	43	43	43							

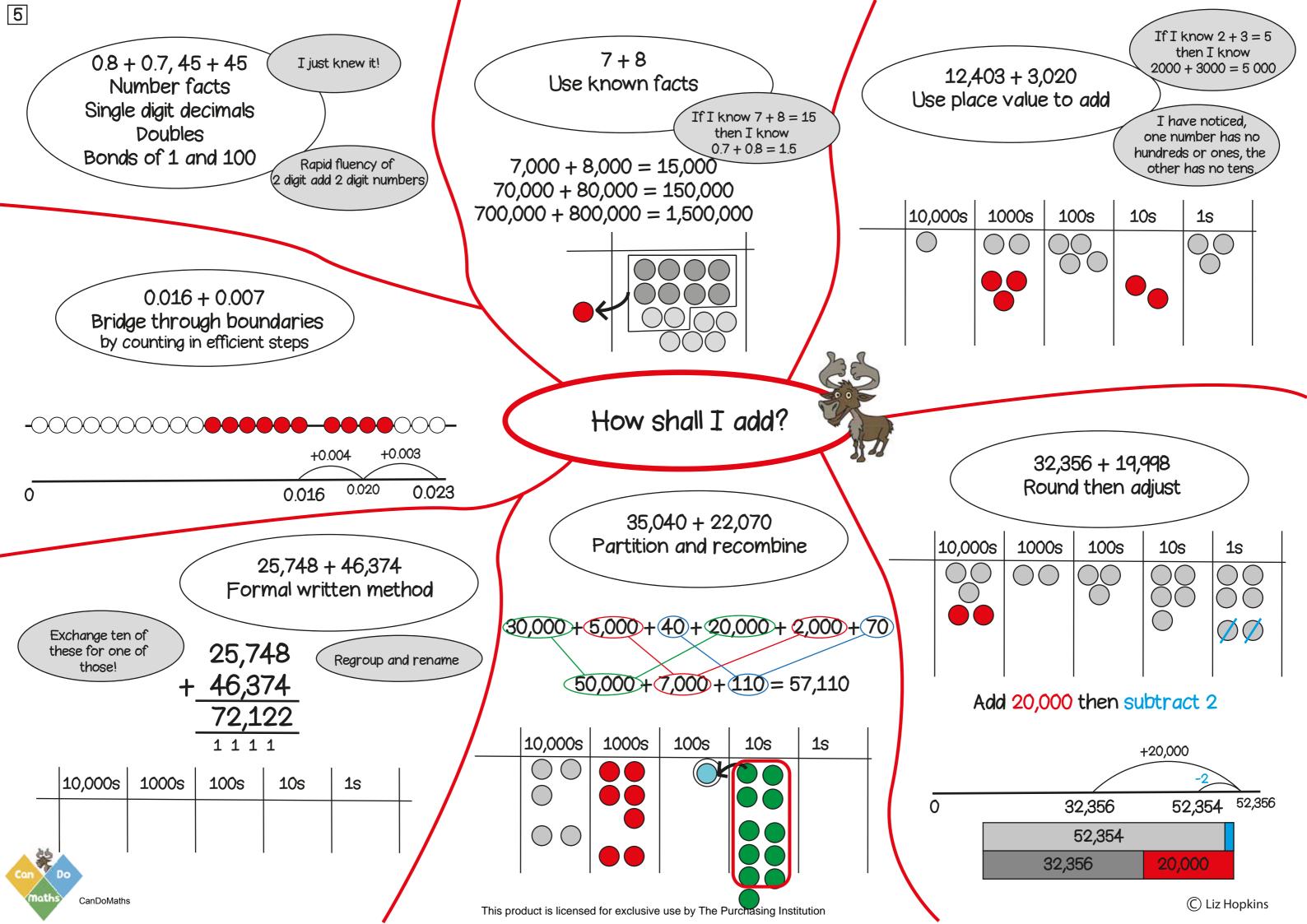


496 ÷ 8 Partition and recombine

60 x 8







9 - 4, 13 - 5, 18 - 9

Number facts

Single digit decimals

Halves

Subtract from 1 and 100

I just knew it!

Rapid fluency of

2 digit subtract

2 digit numbers

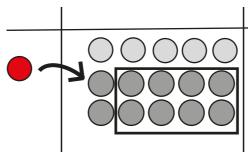
15 - 8 = 7Use known facts

> If I know 15 - 8 = 7 then I know 1.5 - 0.8 = 0.7

15,000 - 8,000 = 7,000

150,000 - 80,000 = 70,000

1,500,000 - 800,000 = 700,000



5 less than 12 is 7 Now it is easy to take away 3000

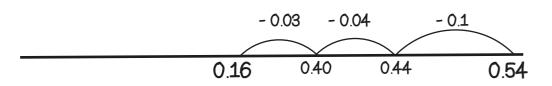
40,012 - 3,005 Use place value to subtract

If I know 40 - 3 = 37
then I know that
40 thousand take away
3 thousand is 37 thousand

40,000 = 4 tens of thousands or 40 thousands 12 = 1 ten and 2 ones or 12 ones

40,012 = 40 thousands and 12 ones take away 3 thousands and 5 ones equals 37 thousands and 7 ones.

0.54 - 0.17
Bridge through boundaries
by counting in efficient steps

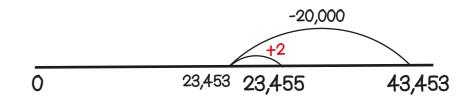


How shall I subtract?

43,453 - 19,998 Round then *adjust*

10,000s	1000s	100s	10s	1s

Take away 20,000 then add 2



45,748 - 26,374 Formal written method

Exchange ten of these for one of those!

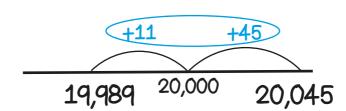
345,748 06 274

Regroup and rename

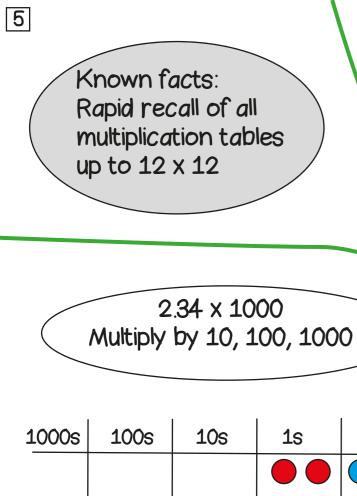
- <u>26,374</u> <u>19,374</u>

10,000s	1000s	100s	10 s	1 s	

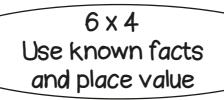
20,045 - 19,989 Find the difference between two numbers

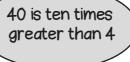


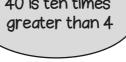
20,045	
19,989	56



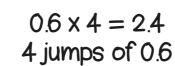
CanDoMaths











0.6 is ten times

smaller than 6

6 x 4

Use known facts

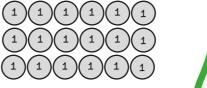
and place value

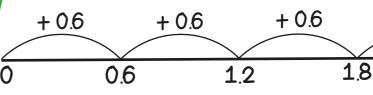
0.6

+ 0.6

2.4

1

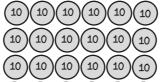




 $6 \times 4 = 24$

 $60 \times 4 = 240$

 $60 \times 40 = 2400$



$0.6 \times 0.4 = 24$ hundredths $0.6 \times 0.4 = 0.24$

0.4



x10

x10

/ x10

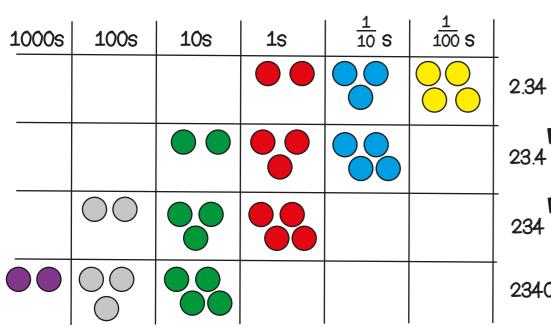
23.4

234

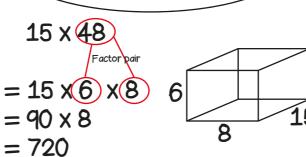
2340

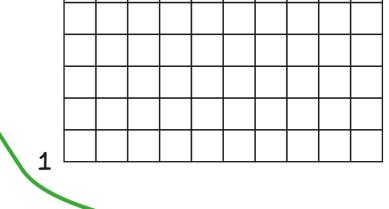


How shall I multiply?

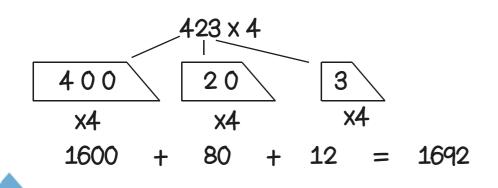


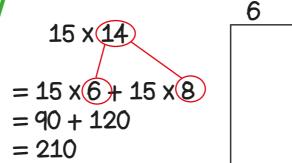


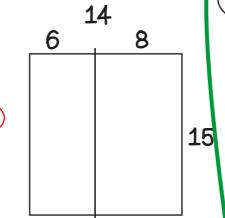




423 x 4 Partition and recombine







427 x 38 Formal written method

	400	20	7
30	12,000	600	210
8	3,200	160	56

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5 Known facts: Use recall of all multiplication tables

up to 12 x 12 to

derive division facts

24 ÷ 1000

Divide by 10, 100, 1000

Include calcuations where remainders occur

24 ÷ 4 Use known facts

and place value

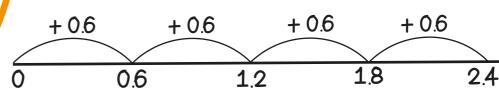
24,000 is a thousand times greater than 24

0.6 is ten times smaller than 6

 $2.4 \div 0.6$ Use known facts and place value

$$2.4 \div 0.6 = 4$$

How many steps of 0.6 make 2.4?



5724 ÷ 4

Formal written method

1000s 100s

 $24 \div 4 = 6$ $240 \div 40 = 6$

 $2400 \div 400 = 6$

 $24,000 \div 4000 = 6$

If there are 1000 times as many people and 1000 times as many biscuits, how many biscuits each now?

24 biscuits shared between

4 people means they will get

6 biscuits each.

$$24,000 \div 400 = \underbrace{24 \times 1000}_{4 \times 100}$$

$$\frac{4}{240} = 60$$

2 x 8

496

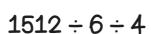
480

÷1000

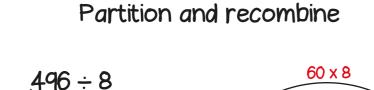
$\frac{1}{10}$ s $\frac{1}{100}$ s $\frac{1}{1000}$ s 100s

How shall I divide?

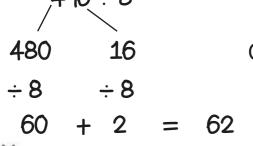
1512 ÷ 24 Using factors



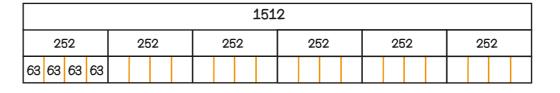
 	 100	1000	10000	
				24) ÷10
				2.4) ÷10
				0.24)÷10
		00		0.024



496 ÷ 8



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44 + 56, 27 + 27 Number facts Single digit decimals Doubles Bonds of 1 and 100

I just knew it!

Rapid fluency of 2 digit add 2 digit numbers

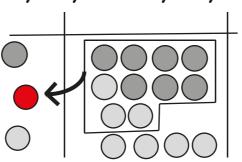
17 + 17 Use known facts

> If I know 17 + 17 = 34then I know 1.7 + 1.7 = 3.4

17,000 + 17,000 = 34,000

170,000 + 170,000 = 340,000

1,700,000 + 1,700,000 = 3,400,000

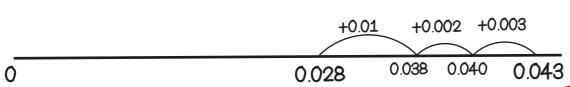


1,102,403 + 50,020 Use place value to add

I have noticed, one number has no hundreds or ones, the other has no tens

1,000,000s	100,000s	10,000s	1000s	100s	10s	1 s
				00		00

0.028 + 0.015 Bridge through boundaries by counting in efficient steps



325,748 + 246,374 Formal written method

Regroup and rename

Exchange ten of these for one of those!

325,748 + 246,374 572,122

100,000s	10,000s	1000s	100s	10 s	1 s	

How shall I add?

307,040 + 206,070 Partition and recombine

300,000 + 7,000 + 40 + 200,000 + 6,000 + 70

500,000 + 13,000 + 110 = 513,110

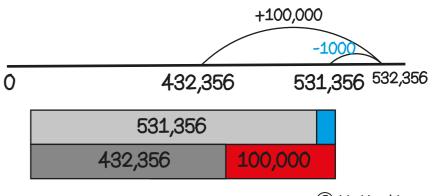
100s 10s 1s	100s	1000s	10,000s	100,000s
	'			

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432,356 + 99,000 Round then adjust

100,000s	10,000s	1000s	100s	10s	1 s
	00	Ø		000	000

Add 100,000 then take away 1,000



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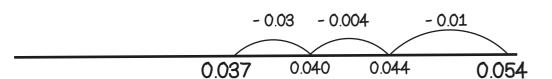
0.9 - 0.4, 100 - 65 (
Number facts
Single digit decimals
Halves
Bonds of 1 and 100

Rapid fluency of 2 digit subtract 2 digit numbers

I just knew it!

0.054 - 0.017

Bridge through boundaries by counting in efficient steps



445,748 - 126,374 Formal written method

Exchange ten of these for one of those!

CanDoMaths

445,748 + 126,374

319,374

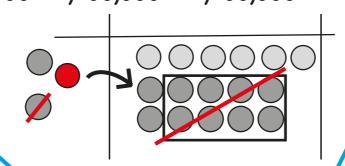
Regroup and rename

100,000s	10,000s	1000s	100s	10s	1 s

36 - 18 = 18Use known facts

> If I know 36 - 18 = 18 then I know 3.6 - 1.8 = 1.8

36,000 - 18,000 = 18,000 360,000 - 180,000 = 180,000 3,600,000 - 1,800,000 = 1,800,000



400,032 - 30,005 (Use place value to subtract 5 less than 32 is 27

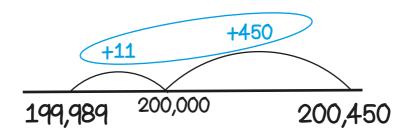
400,000 = 4 hundreds of thousands or 400 thousands

400 - 30 = 370 so 400,000 - 3,000 = 370,000

400,032 = 400 thousands and 32 ones take away 30 thousands and 5 ones = 370,027

How shall I subtract?

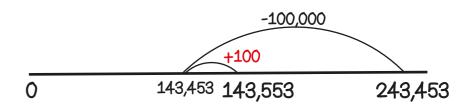
200,450 - 199,989 Find the difference between two numbers

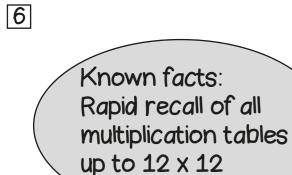


200,450 199,989 461 243,453 - 99,900 Round then adjust

	_		_	_	_	
100,000s	10,000s	1000s	100s	10s	1s	
Ø	00				00	

Take away 100,000 then add 100





6 x 4 Use known facts and place value

x10

x10

40 is ten times greater than 4

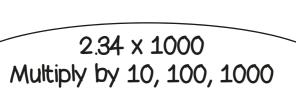
$$60 \times 40 = 2400$$

 $600 \times 400 = 240,000$

 $6000 \times 4000 = 240,000$ $6000 \times 4000 = 24,000,000$

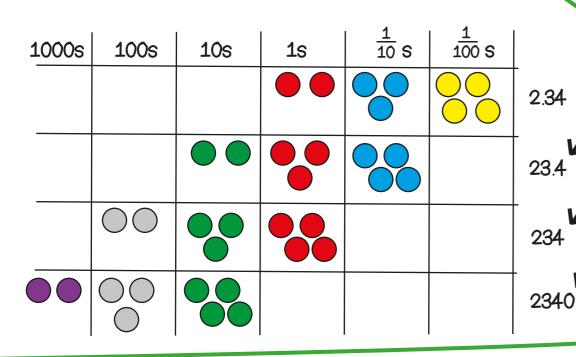
 $6 \times 10 \times 4 \times 10$ = 24 × 100

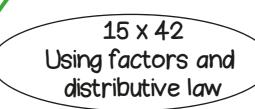
x100





How shall I multiply?

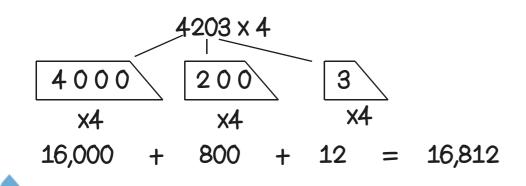


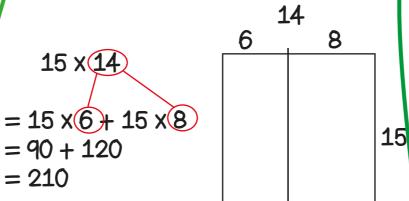


15 x 48 = 15 x 6 x 8 6 = 90 x 8 = 720

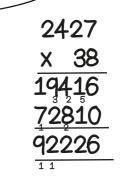
4203 x 4 Partition and recombine

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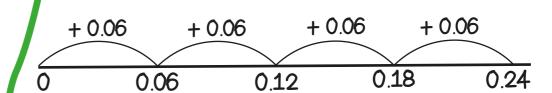
2427 x 38 Formal written method



and place value 0.06 x 4 = 0.24 4 jumps of 0.06

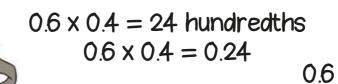
0.6 is ten times

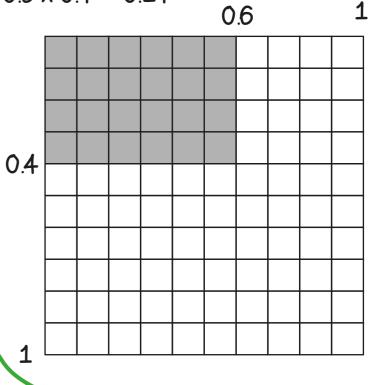
smaller than 6



6 x 4

Use known facts





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Known facts: Use recall of all multiplication tables up to 12 x 12 to derive division facts

6

Include calcuations where remainders occur

 $24 \div 4$

Use known facts and place value

240 is ten times greater than 24

24 biscuits shared between

4 people means they will get

people and 10 times as many

6 biscuits each.

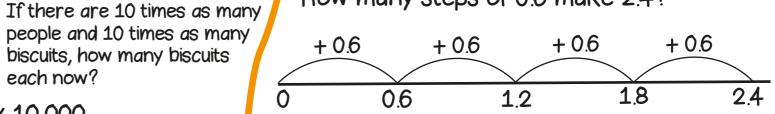
smaller than 6

0.6 is ten times

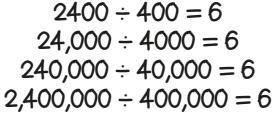
 $2.4 \div 0.6$ Use known facts and place value

$$2.4 \div 0.6 = 4$$

How many steps of 0.6 make 2.4?



24 ÷ 1000 Divide by 10, 100, 1000



÷10

 $240 \div 40 = 6$

biscuits, how many biscuits each now? $240,000 \div 400 = 24 \times 10,000$ 4 x 100

$$\frac{2400}{4} = 600$$

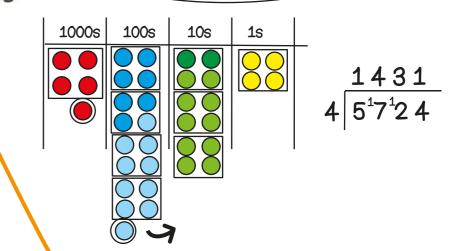
÷1000

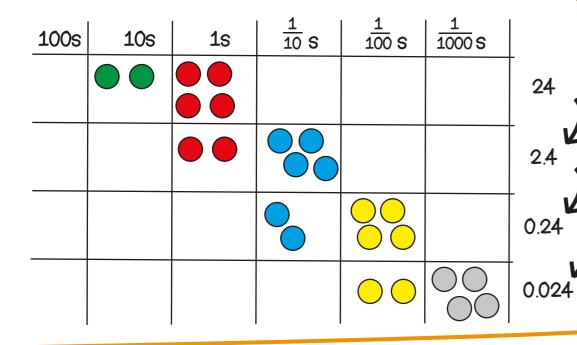
How shall I divide?

1512 ÷ 24

Using factors

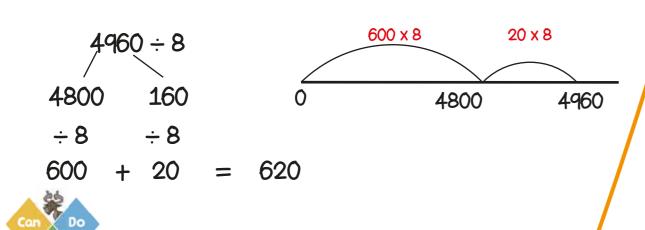
7182 ÷ 21 Formal written method

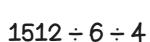




4960 ÷ 8 Partition and recombine

CanDoMaths





1512																							
252				252			252			252			252				252						
63	63	63	63																				